

“Foundation of Mathematics II”

1. Relations

- Type of Relations: Reflexive, Symmetric, Transitive, Anti-Symmetric
- Equivalence Relations, Equivalence Classes, Properties of Equivalence Classes, Partition

2. Ordering

- Partial Order and Total Order
- Least Element and Greatest Element
- Bounded Set: Upper Bound, Lower Bound Least Upper Bound, Greatest Lower Bound
- Complete Set
- Well Ordered Sets

3. The Natural Numbers N

- Peano's Axioms
- Arithmetic of the Natural Number: The Addition on N , The Multiplication on N
- Properties: Associative Law of Addition and Multiplication, Commutative Law of Addition and Multiplication, Distribution Law, Cancellation Law of Addition and Multiplication
- Ordering on N , N is Well Order Set

4. The Integer Number Z

- Construction of Integer
- The Addition and Multiplication on Z
- Properties: Associative Law of Addition and Multiplication, Commutative Law of Addition and Multiplication,
- Ordering on Z
- Embedding

5. Rational Numbers Q

- Construction of the Rational Numbers
- Addition and Multiplication on Q and Its Properties
- Ordering on Q , Dense Order

6. The Real Numbers

- Completeness Property of R

7. The Complex Number \mathbb{C}

- Addition and Multiplication \mathbb{C}

8. Properties of the Integer Numbers

- Divisibility and Primes
- Greatest Common Divisor and Least Common Multiple
- The Fundamental Theorem of Arithmetic

9. Groups

- Binary Operation
- Definitions: Groups, Commutative Group, Subgroup, Order of Group

Books:

1. اساس الرياضيات، تأليف: د. هادي جابر، د. رياض شاكر، د. نادر جورج
2. Fundamental Concepts of Modern Mathematics, by Max D. Larsen